

Capture of Inelastic Dark Matter in the Sun

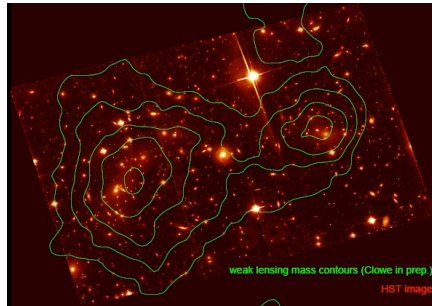
Itay Yavin

Princeton University

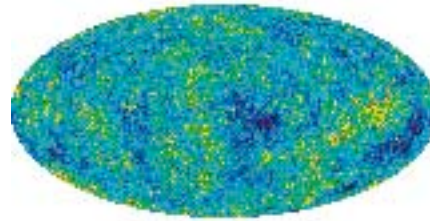
S. Nussinov, L. T. Wang, and I. Y. JCAP08(2009)037, hep-ph 0905.1333

Extended Workshop on DM, Cosmology and the LHC.
Korea, Seoul, August 27th - September 4th

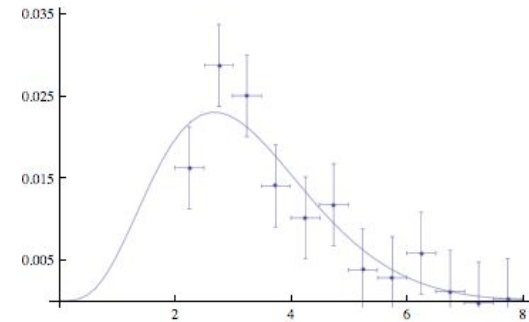
Bullet Cluster



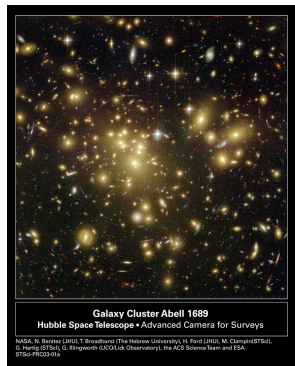
WMAP



Direct Detection

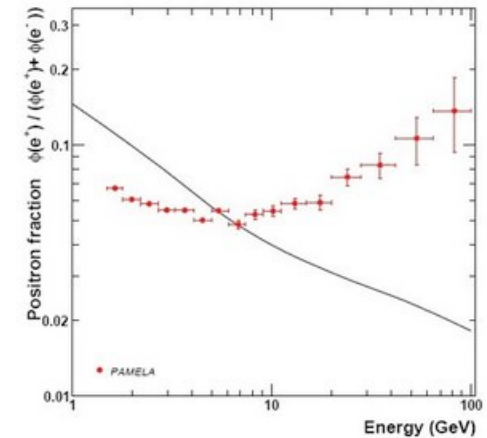


Lensing Effect

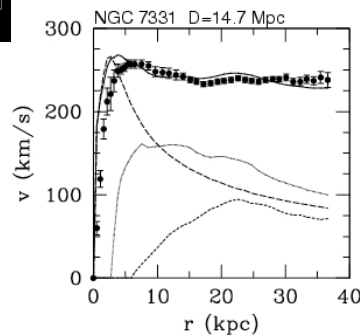


Dark Matter

Indirect Detection



Rotation curves



Direct Production

???

Dark Mass Density

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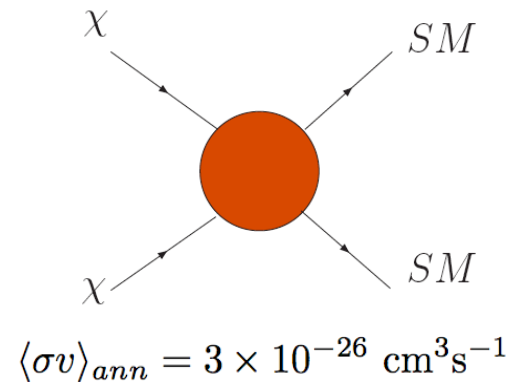
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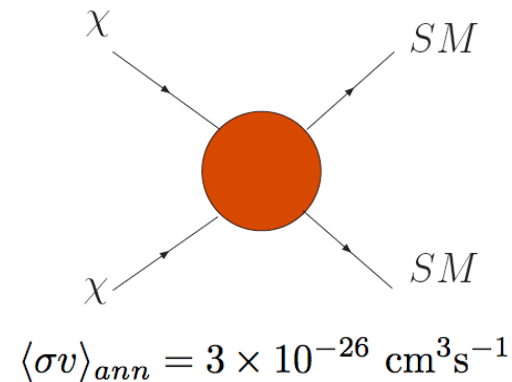
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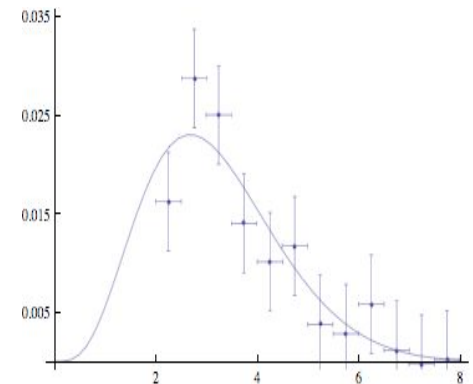
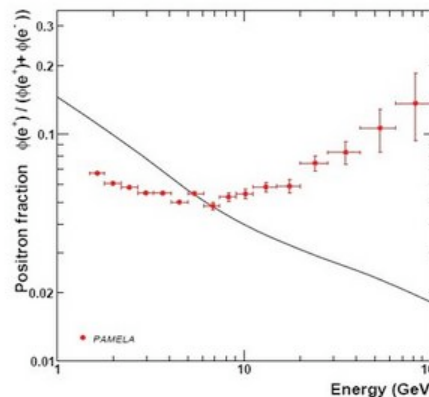
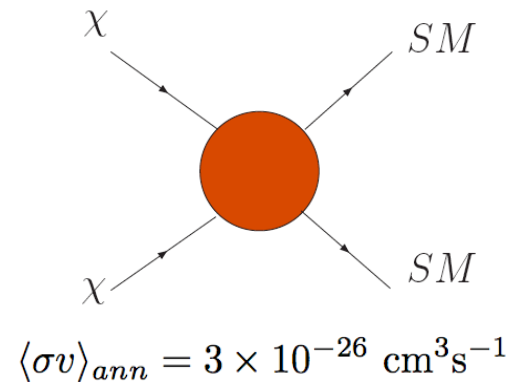
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Capture in the Sun

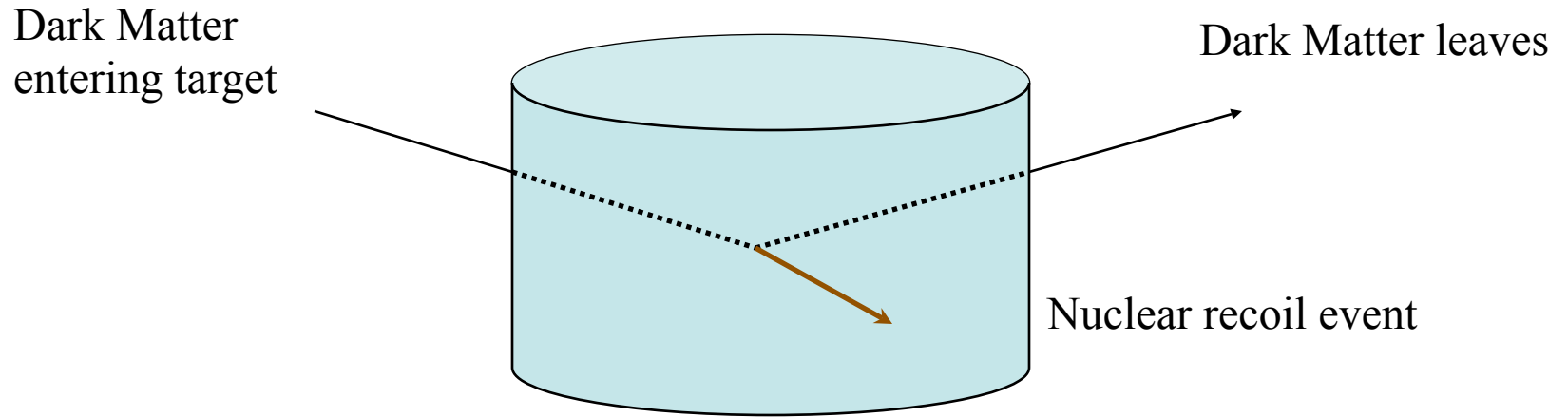
IRAS

Itay Yavin

Content

- Inelastic Dark Matter
- Capture in the Sun
- Inelastic Dark Matter revisited

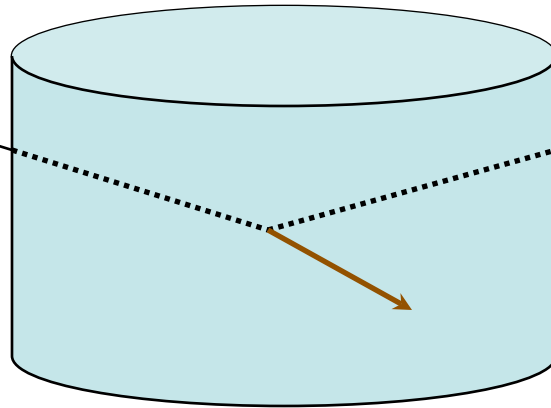
Direct Detection



Direct Detection

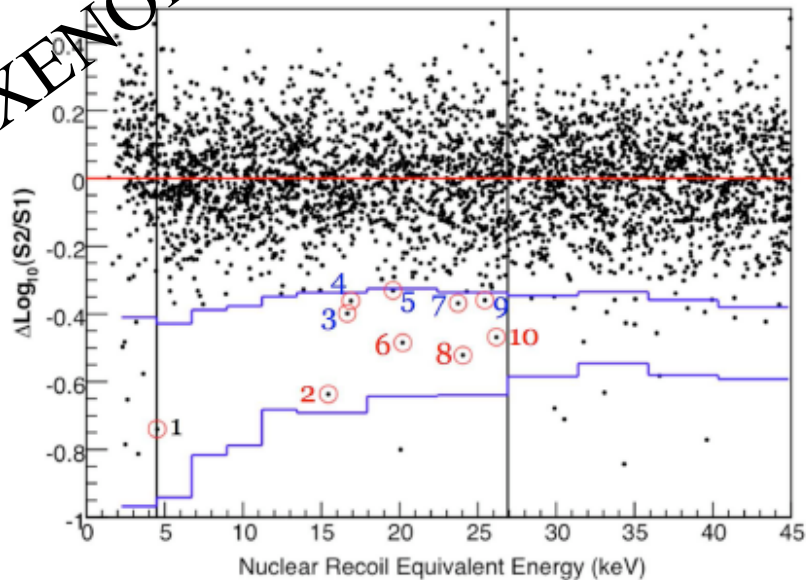
Dark Matter
entering target

Dark Matter leaves



Nuclear recoil event

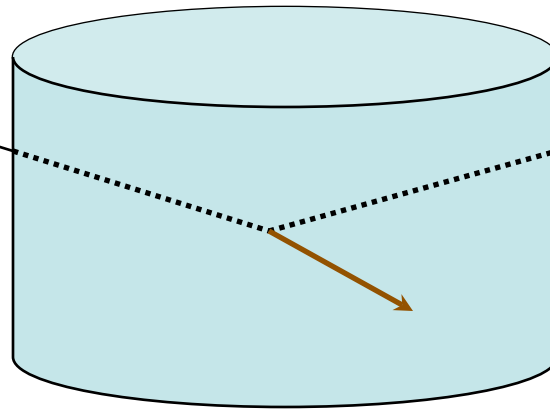
XENON



Direct Detection

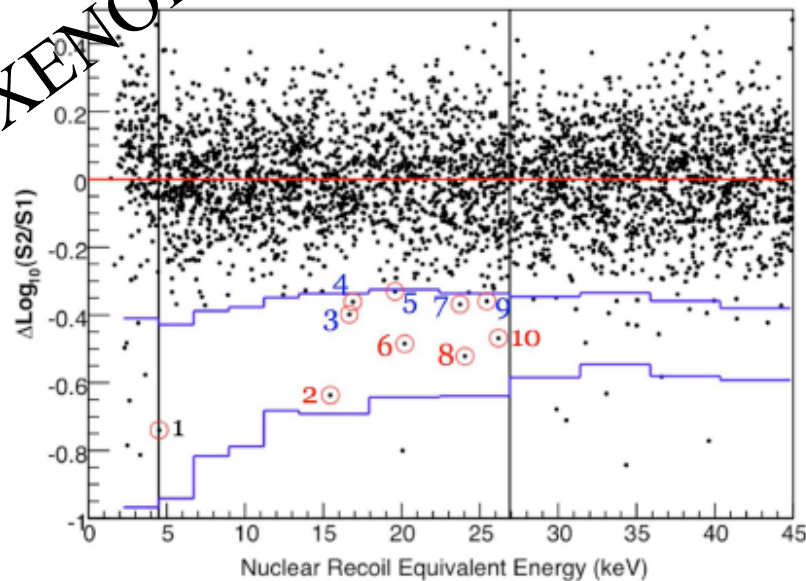
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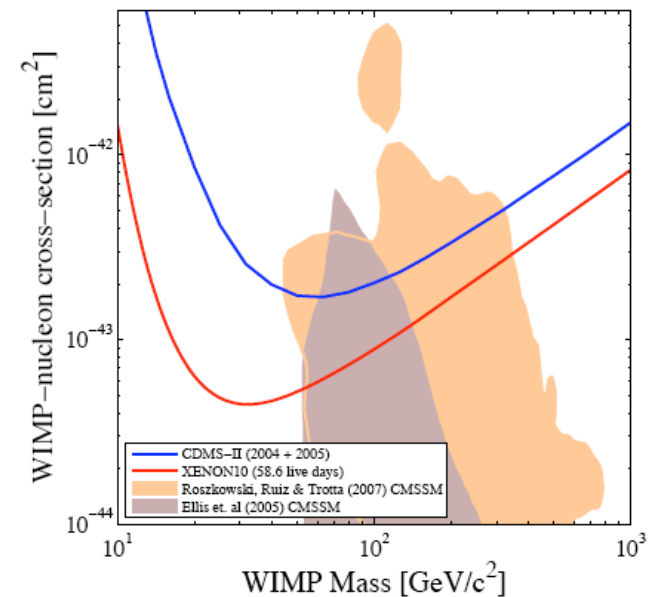


Nuclear recoil event

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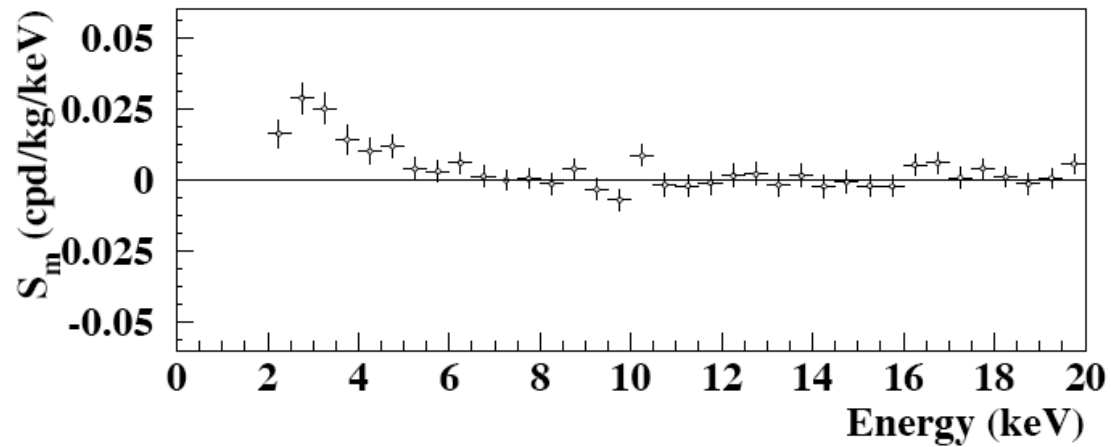
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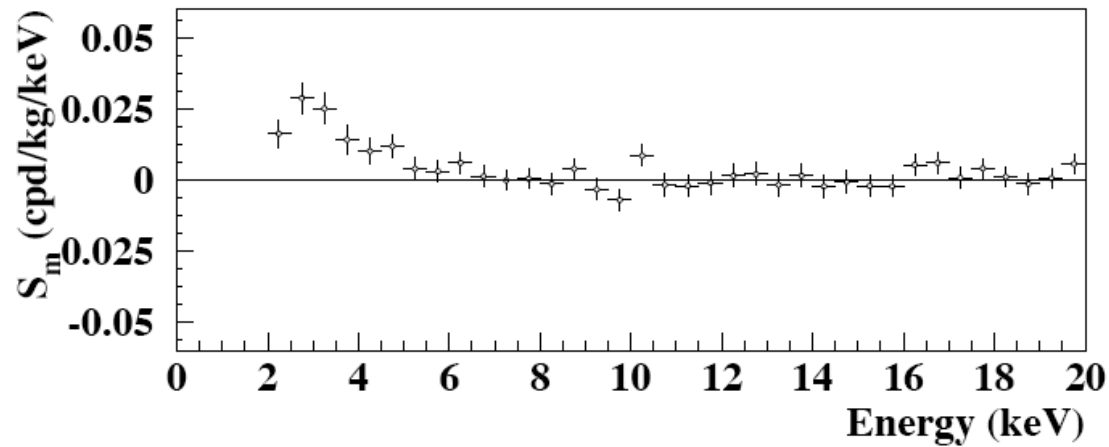
KIAS

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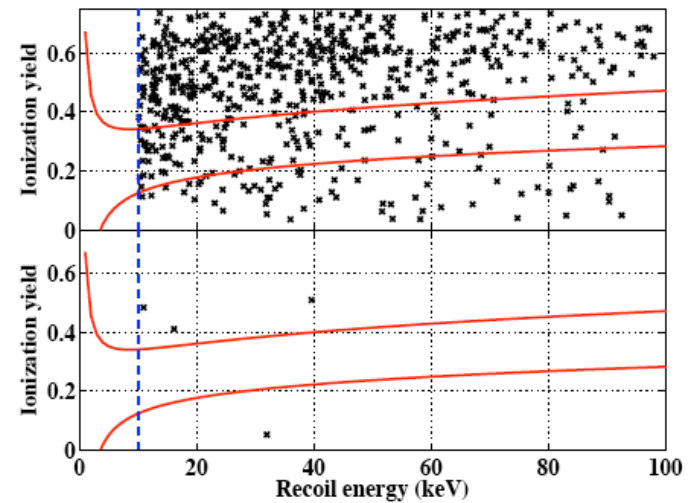
DAMA/LIBRA



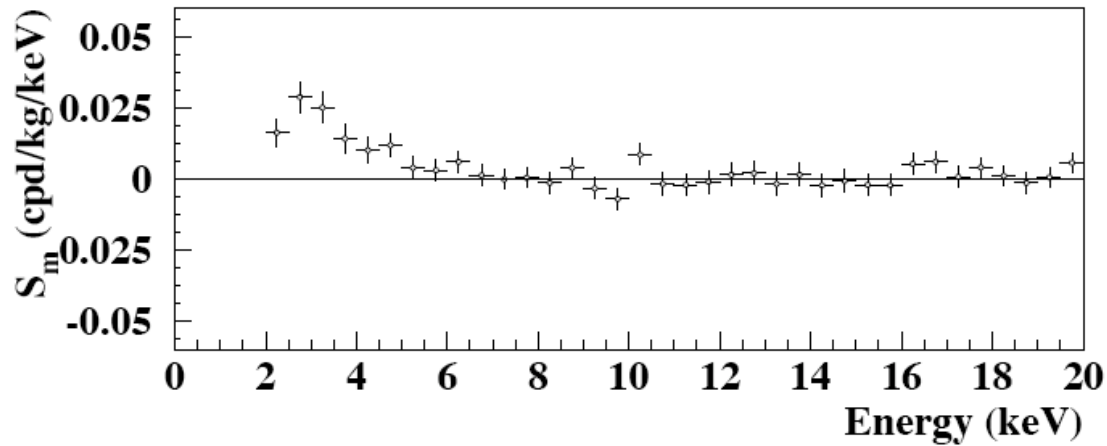
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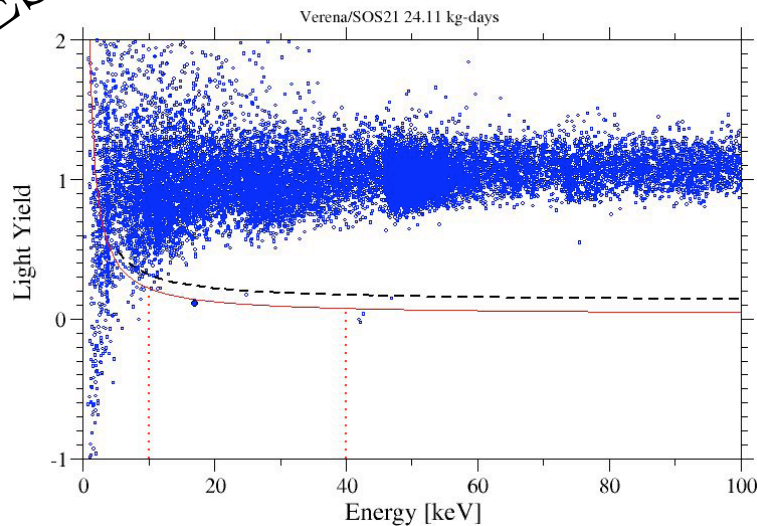
CDMS



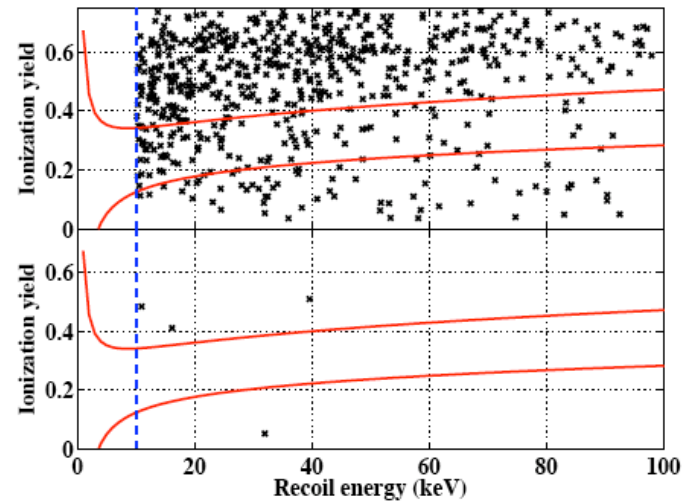
DAMA/LIBRA



CRESST



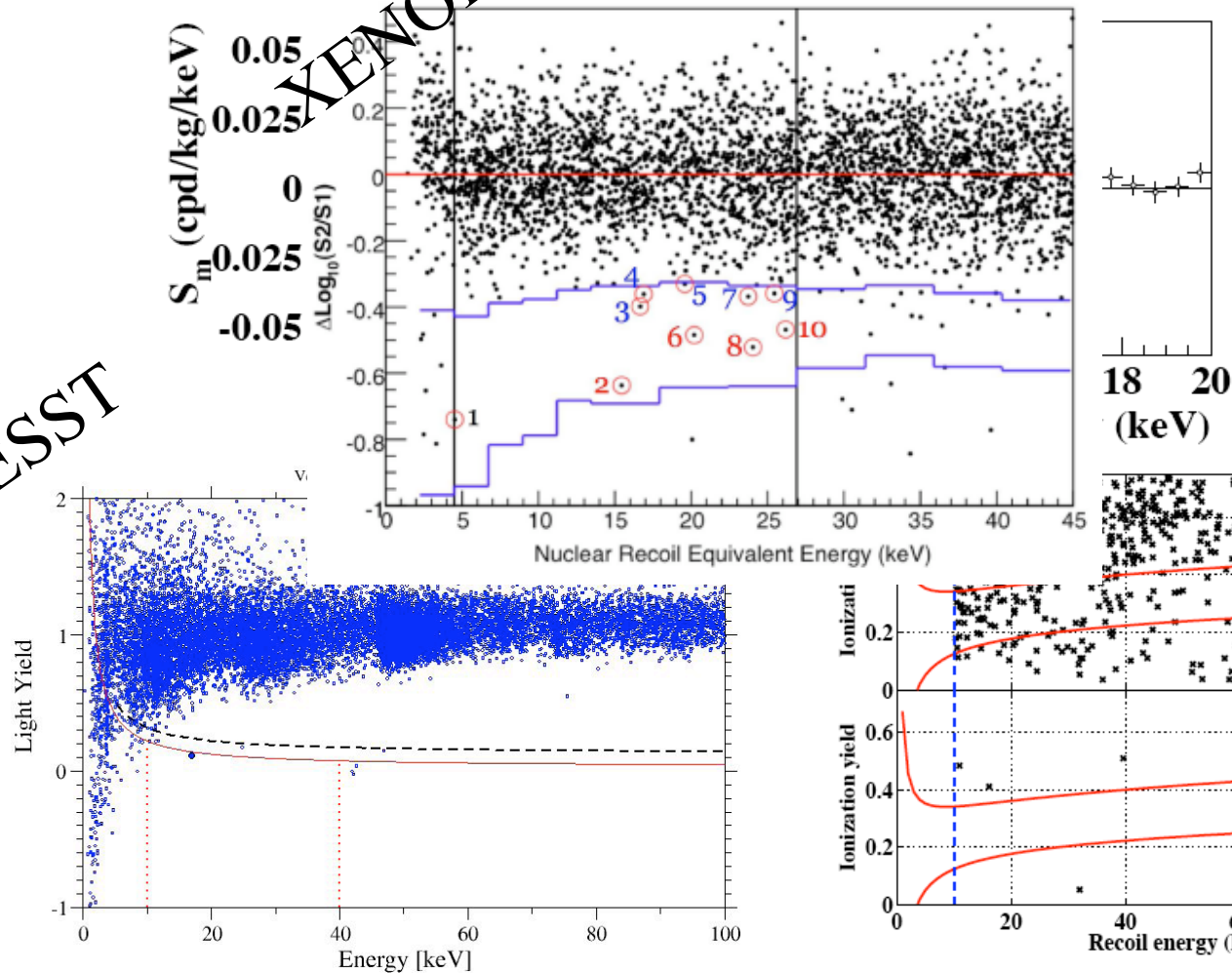
CDMS



DAMA/LIBRA

XENON

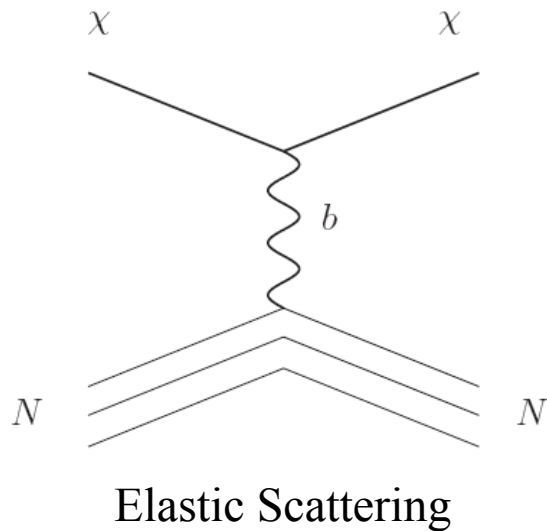
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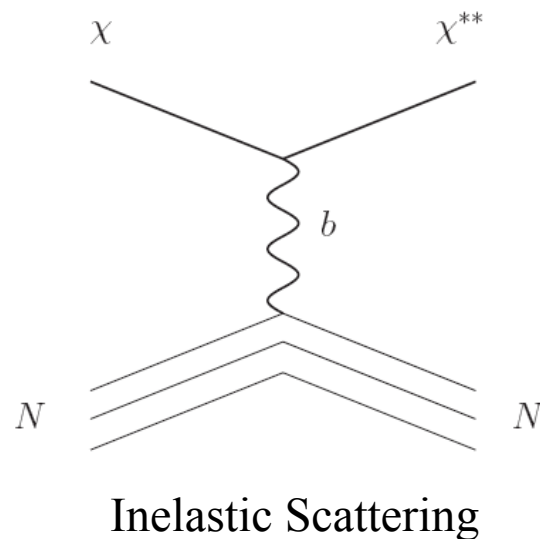
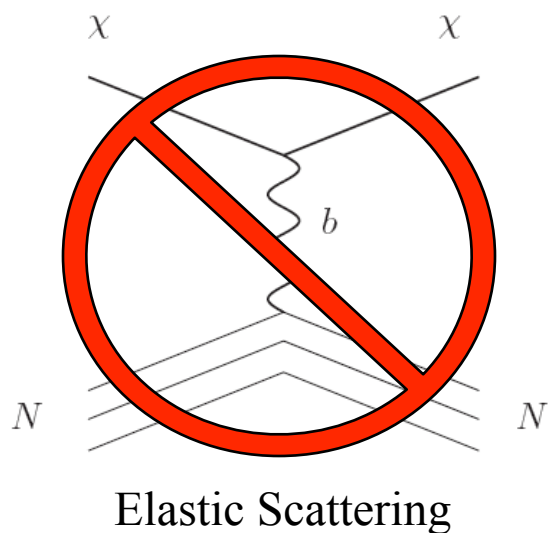
WIMP-Nucleus Recoil

Inelastic DM (**Smith & Weiner**) requires the WIMP to recoil inelastically against the nucleus.



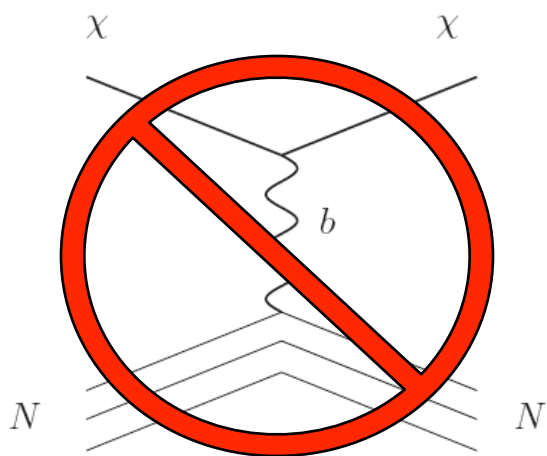
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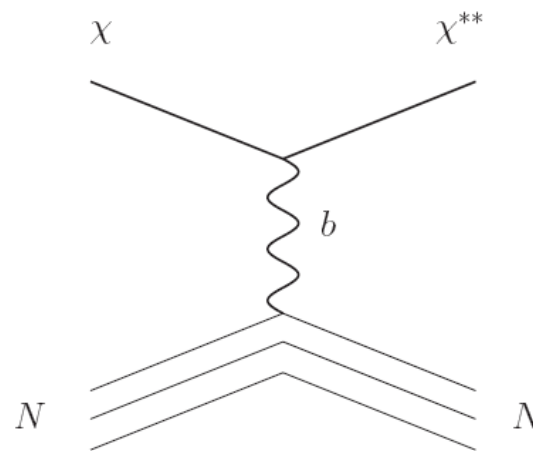


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Elastic Scattering



Inelastic Scattering

$$\beta_{min} = \sqrt{\frac{1}{2m_N E_R} \left(\frac{m_N E_R}{\mu} + \delta \right)}$$

m_N - Nucleus mass

δ - Excitation Energy

E_R - Recoil Energy

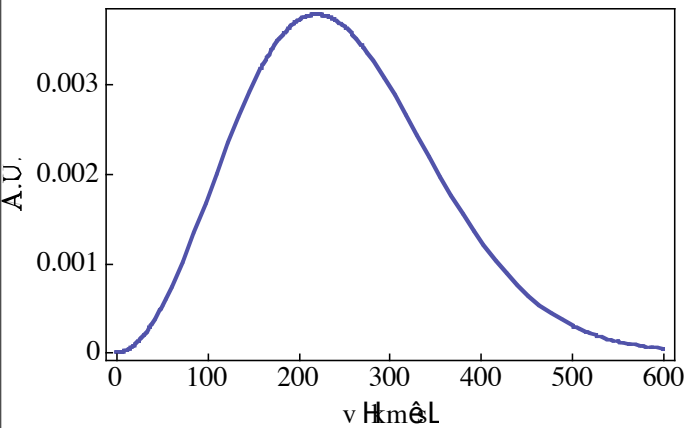
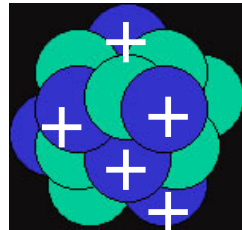
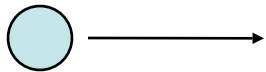
μ - Nucleus-WIMP reduced mass

Inelastic Transitions

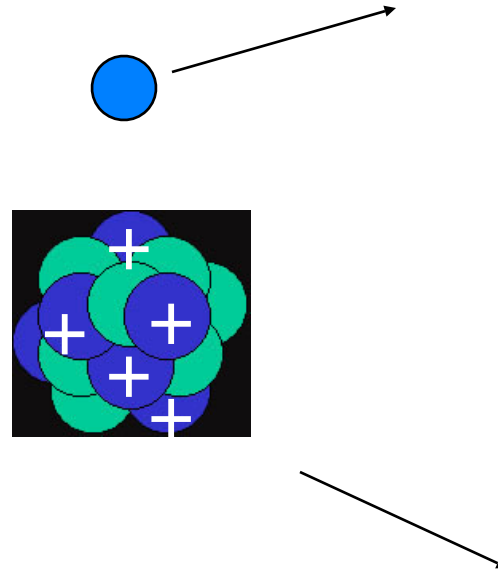
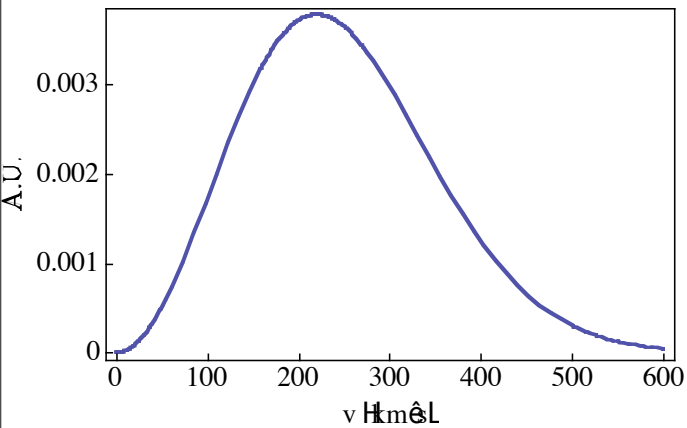
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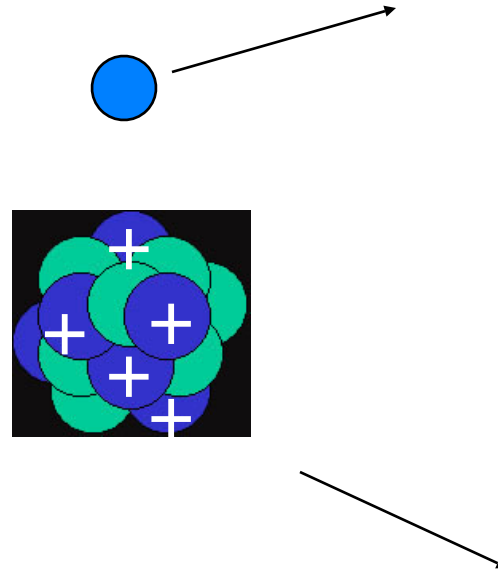
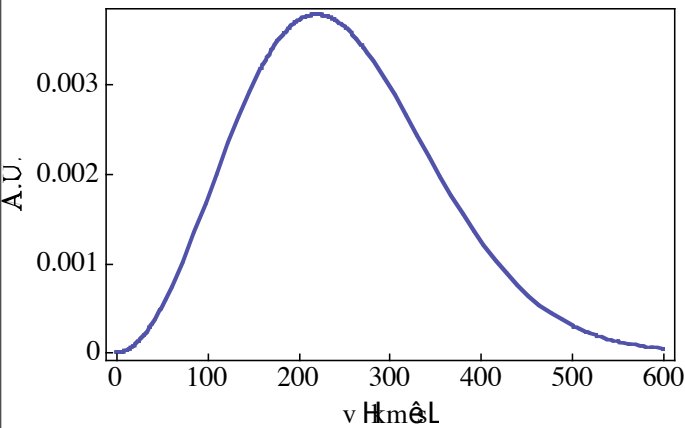
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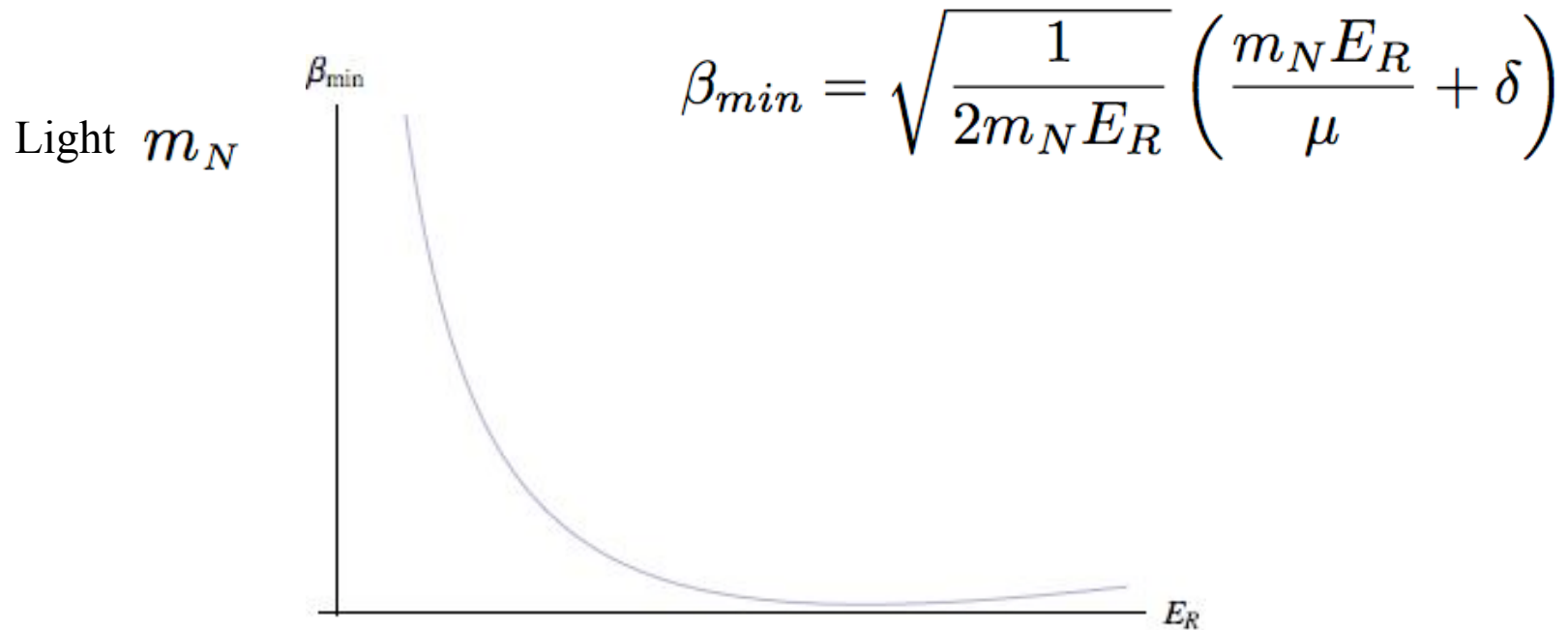


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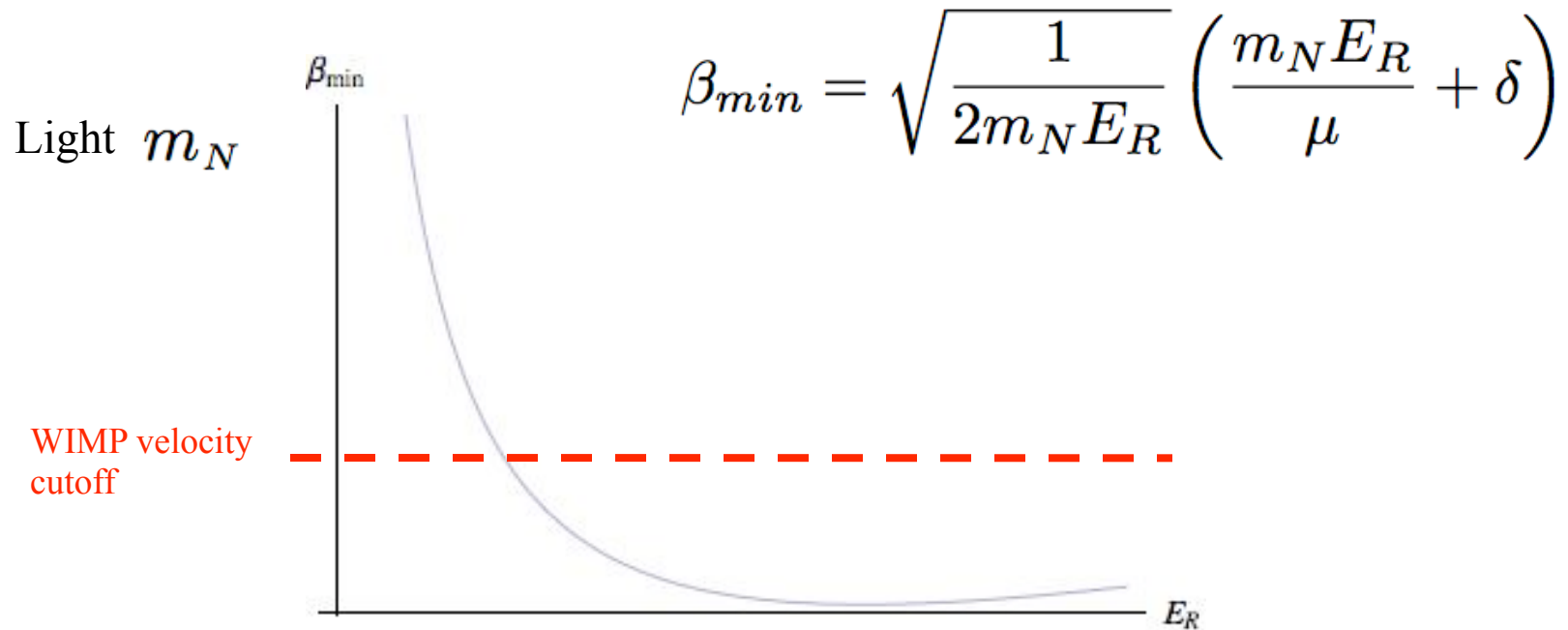


- 1) Light element experiments may not see anything.
- 2) The spectrum of events has a maximum.
- 3) Probing the tail of the Boltzmann distribution ---> large modulations.

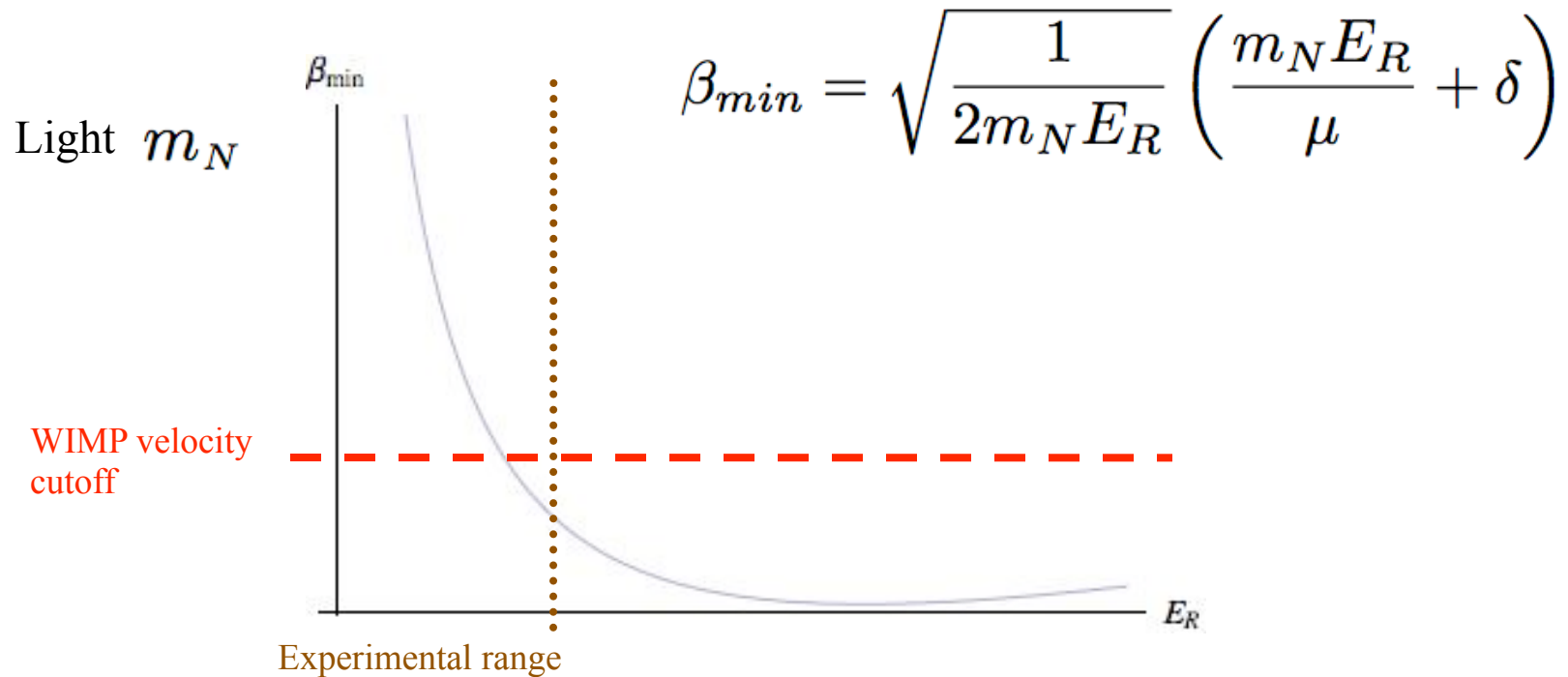
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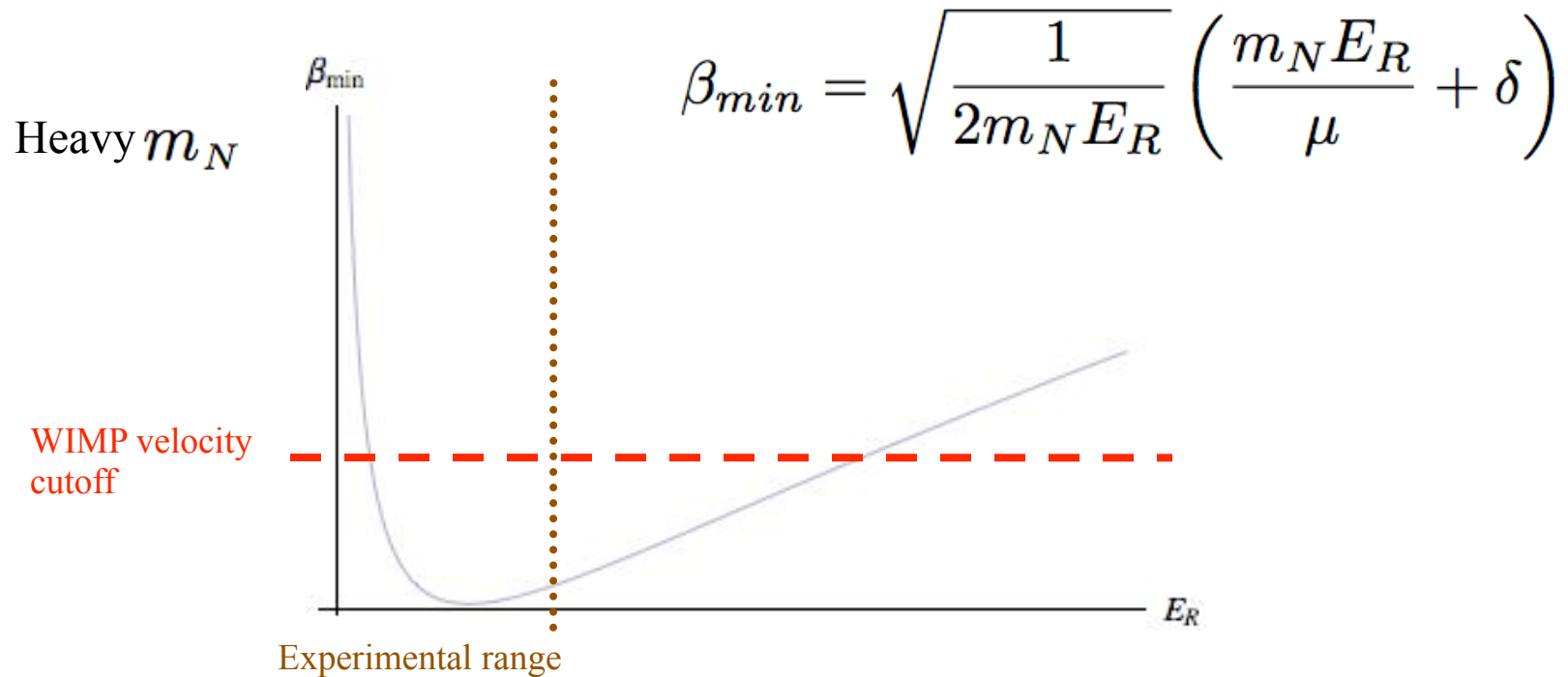
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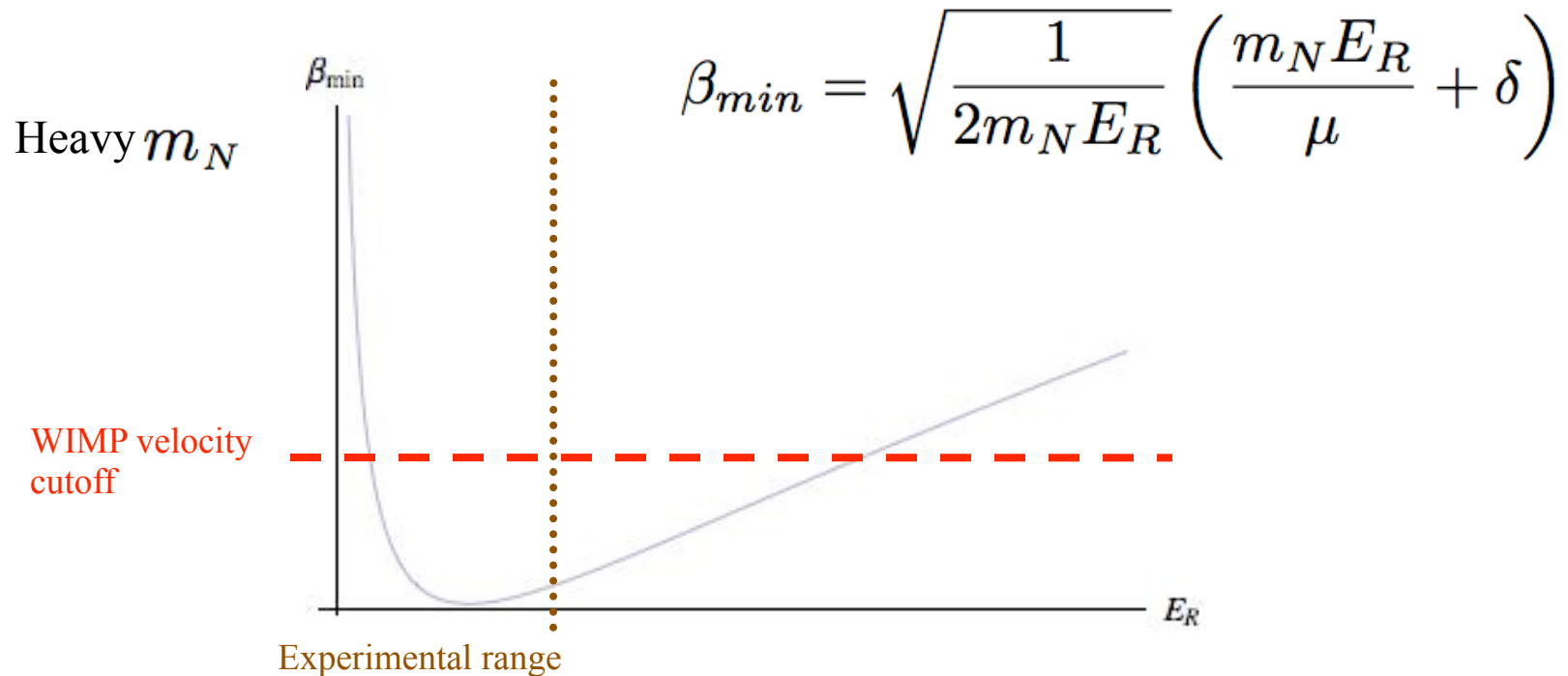
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Fit to DAMA

The differential event rate is given by,

$$\frac{dR}{dE_R} = N_T m_N \frac{\rho_\chi \sigma_n Q^2}{2m_\chi \mu_{ne}^2} F^2(E_R) \int_{\beta_{min}}^{\infty} \frac{f(v)}{v} dv$$

N_T # Nuclear Targets

σ_n Nucleus Mass

m_χ WIMP Mass

μ_{ne} WIMP-nucleon reduced mass

$\rho_\chi = 0.3 \text{ GeV cm}^{-3}$ WIMP mass density

$F^2(E_R)$ Nuclear Form Factor

$f(v)$ WIMP velocity distribution

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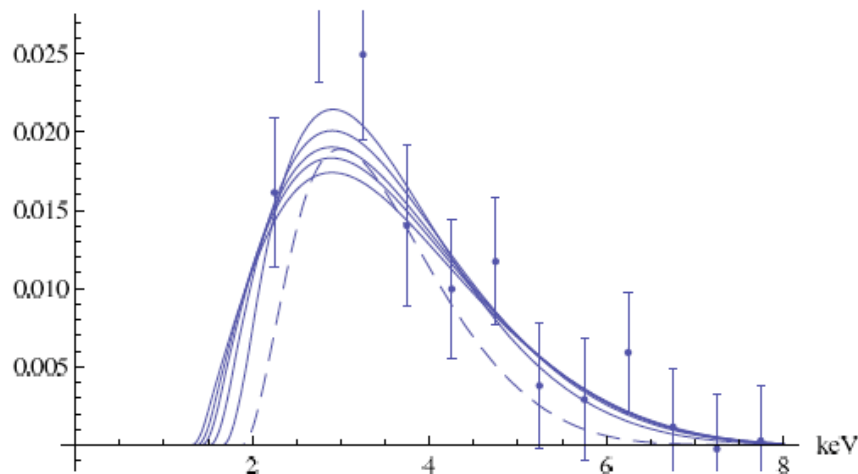
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Capture in the Sun

KIAS

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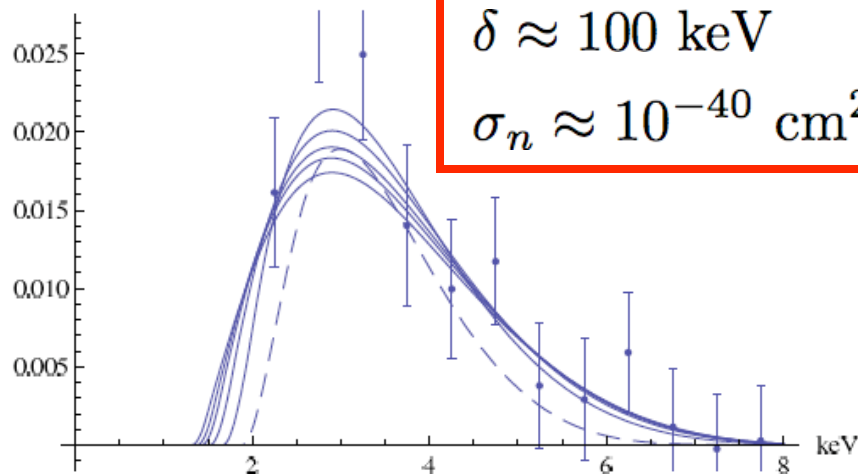
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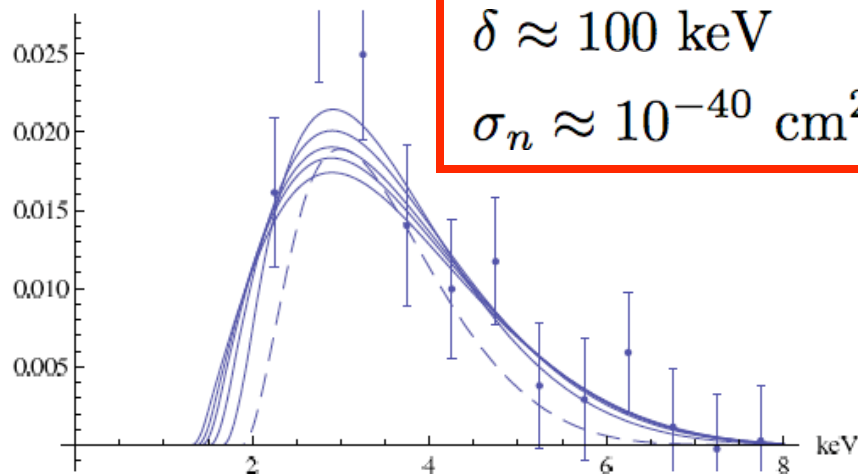
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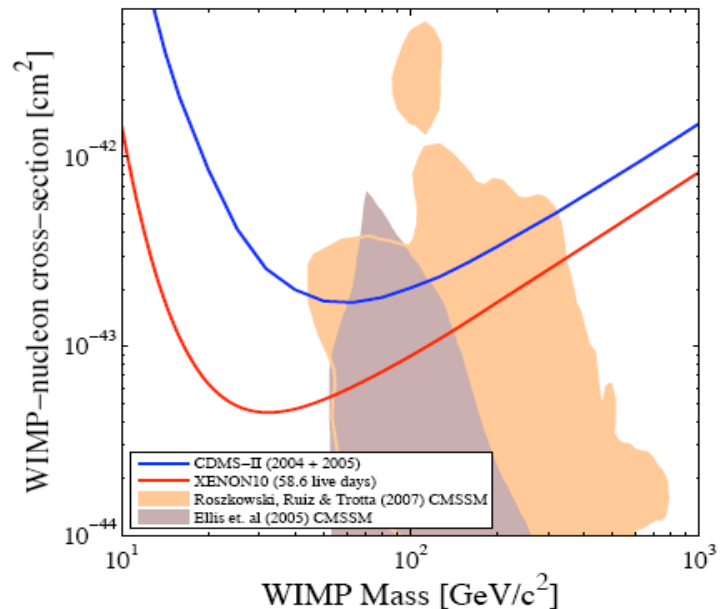
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WIMP Mass [GeV/c²]

Biggest Targets

The biggest effective targets available for us to capture WIMPs are the **Earth** and the **Sun**:

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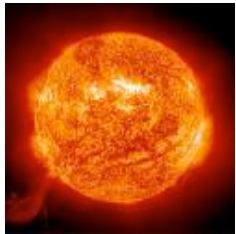
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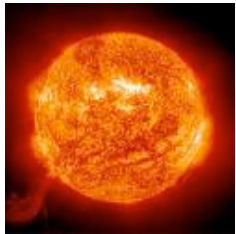


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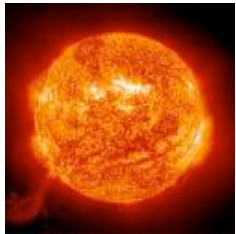
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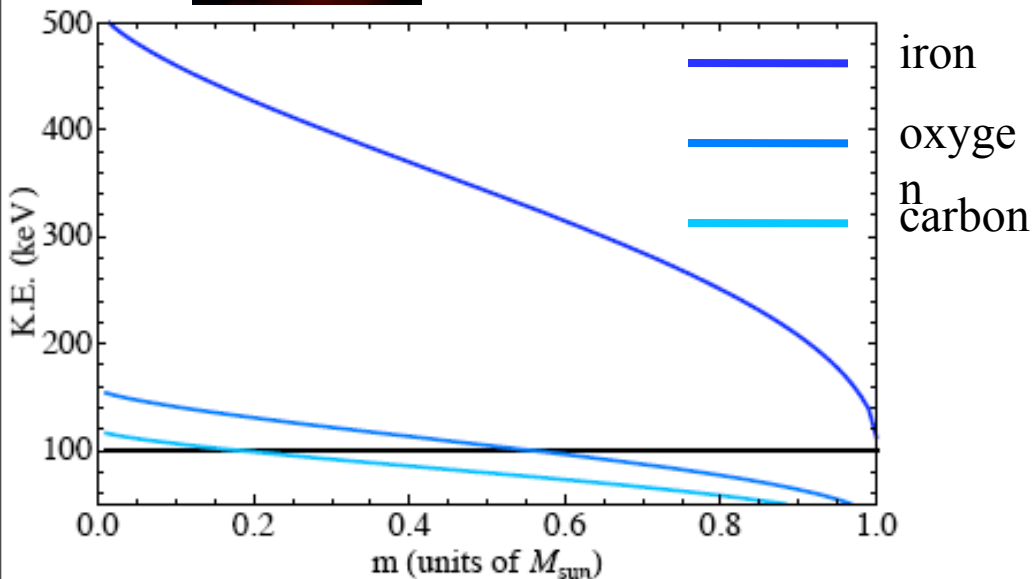
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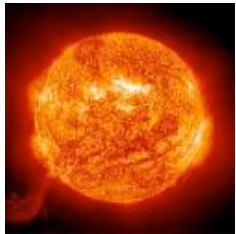


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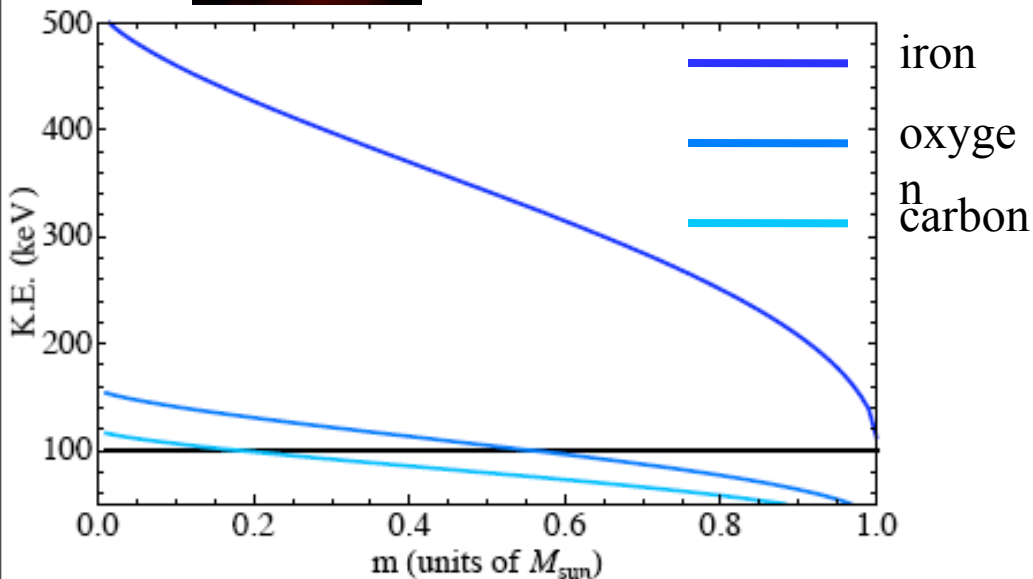
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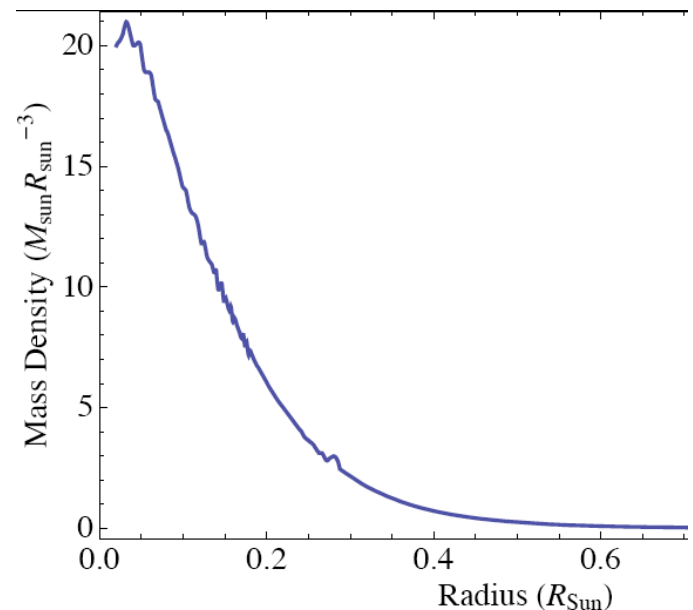
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Capture in the Sun



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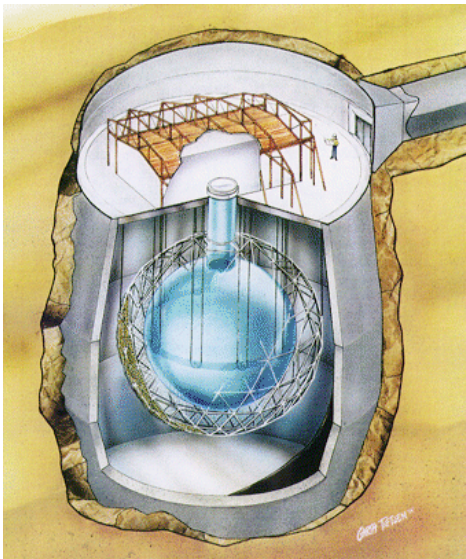
Itay Yavin

Detecting the Captured WIMPs

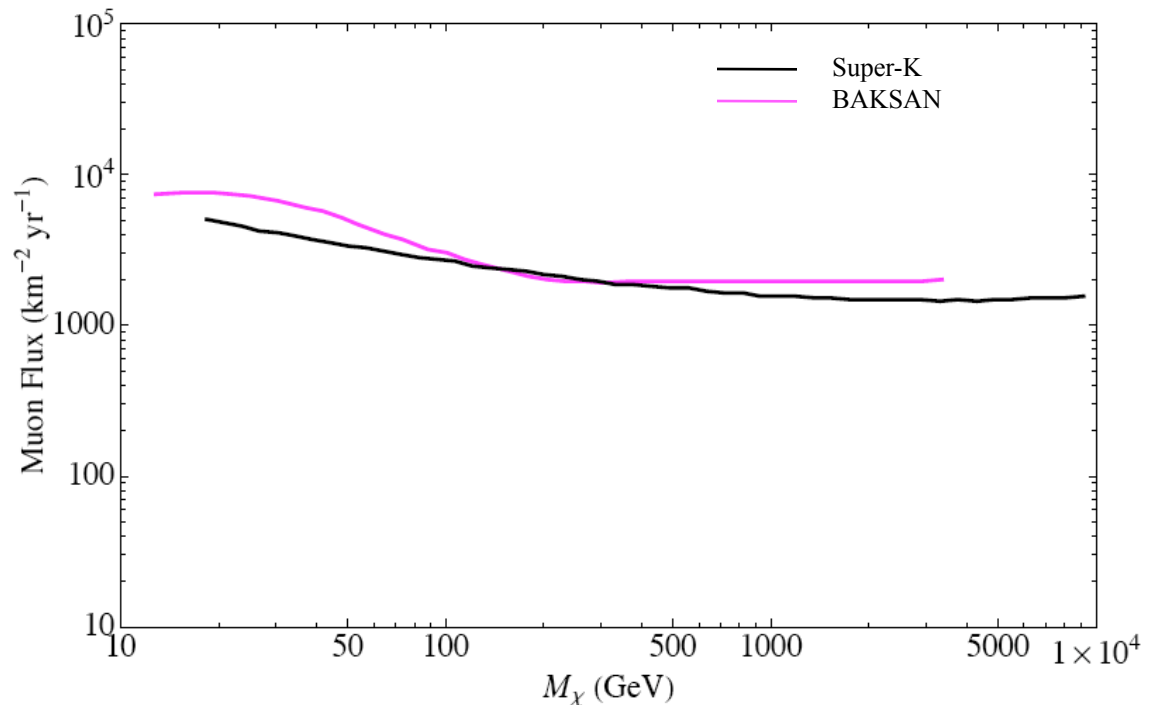
After they get captured, the WIMPs might eventually find each other and annihilate. If the annihilation products contain neutrinos, we can try to detect this flux coming from the Sun:

Underground Detectors: Observing the incoming neutrino through its conversion into a charged lepton and the subsequent .

Neutrino Telescopes: A muon-neutrino converts into a muon in the rock (or ice, or water) below the detector. The muon is subsequently detected with a large sparse array (Ice-Cube, Antares).



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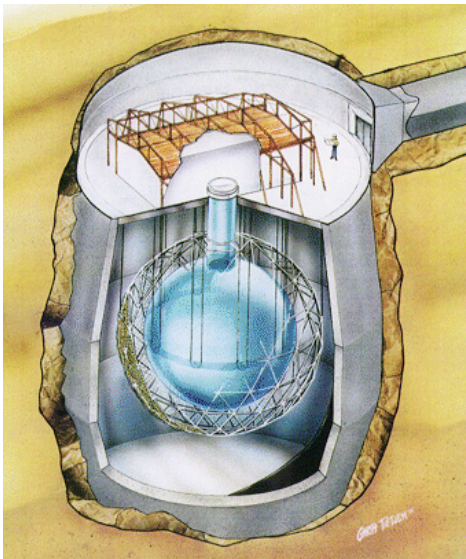
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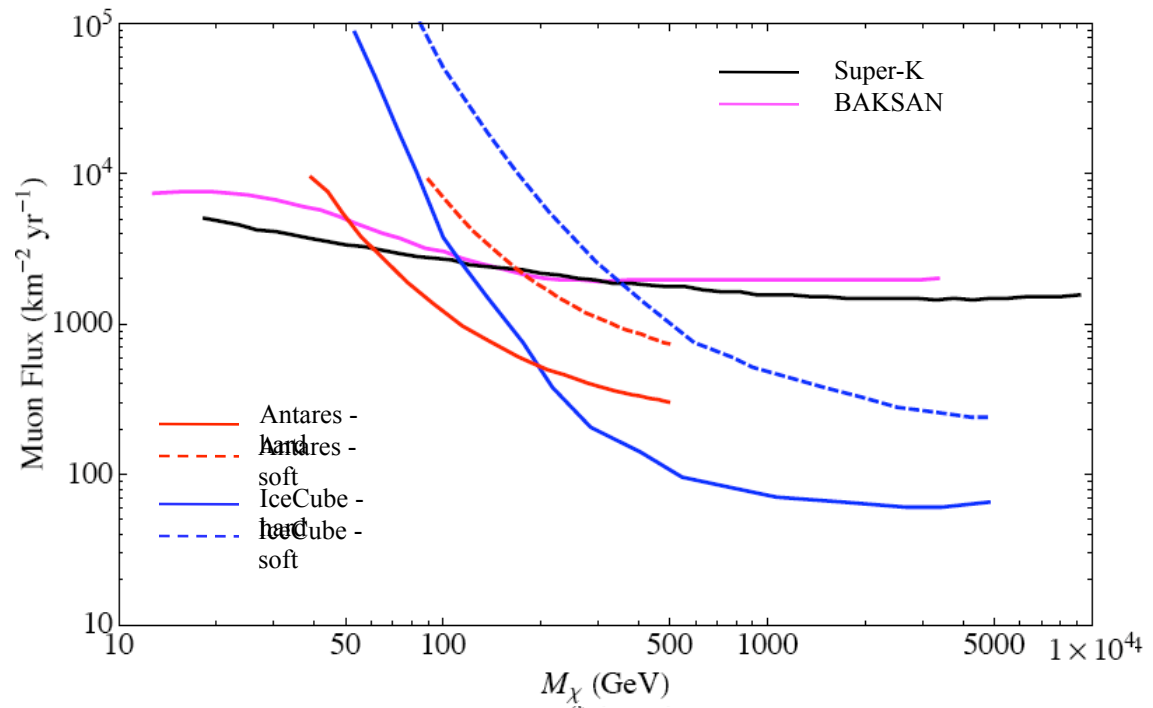
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How to Compute Muon Flux

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Capture Rate
(WIMP/sec)

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Muon Flux
(muon/sec/area)

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WIMP velocity
distribution 4

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Properties of
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WIMP-nucleus
cross-section 6

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(muon/sec/area)

How to Compute Muon Flux

The computation can be separated into logically disjoint modules, as follows:

WIMP-nucleus
cross-section 6

WIMP velocity
distribution 4

Capture Rate
(WIMP/sec)

Properties of
the Sun 4

Kinematics 6

Annihilation
cross-section 4

Annihilation Rate
(Neutrinos/sec)

Annihilation
products 6

WIMP
density 6

Muon Flux
(muon/sec/area)

Many many things 4

Capture Rate - Back of the Envelope

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$$\sigma = \frac{4m_N m_\chi}{(m_\chi + m_N)^2} \left(\frac{m_N m_\chi}{\text{GeV}^2} \right) Q^2 \sigma_n$$

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Capture in the Sun

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KIAS

Itay Yavin

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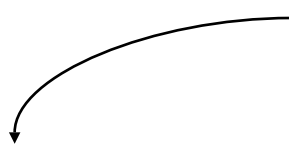
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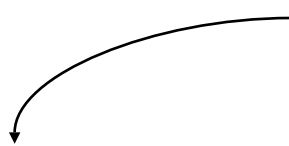
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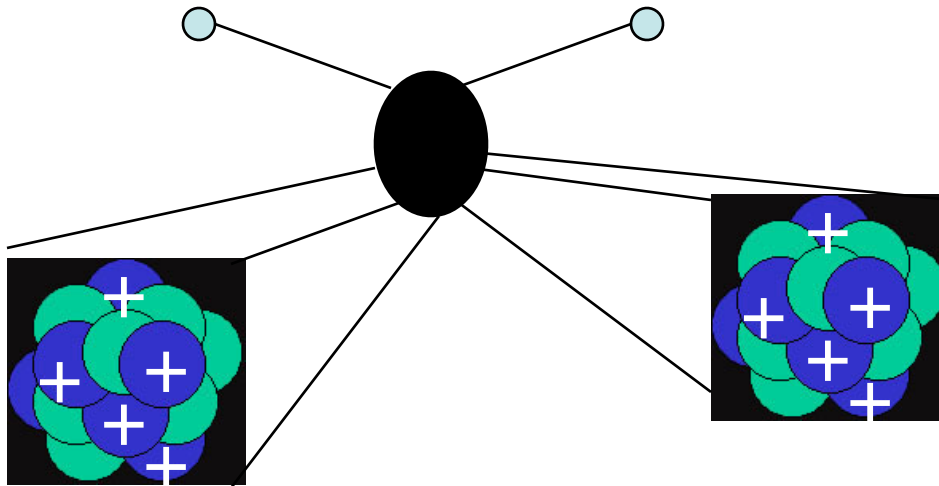
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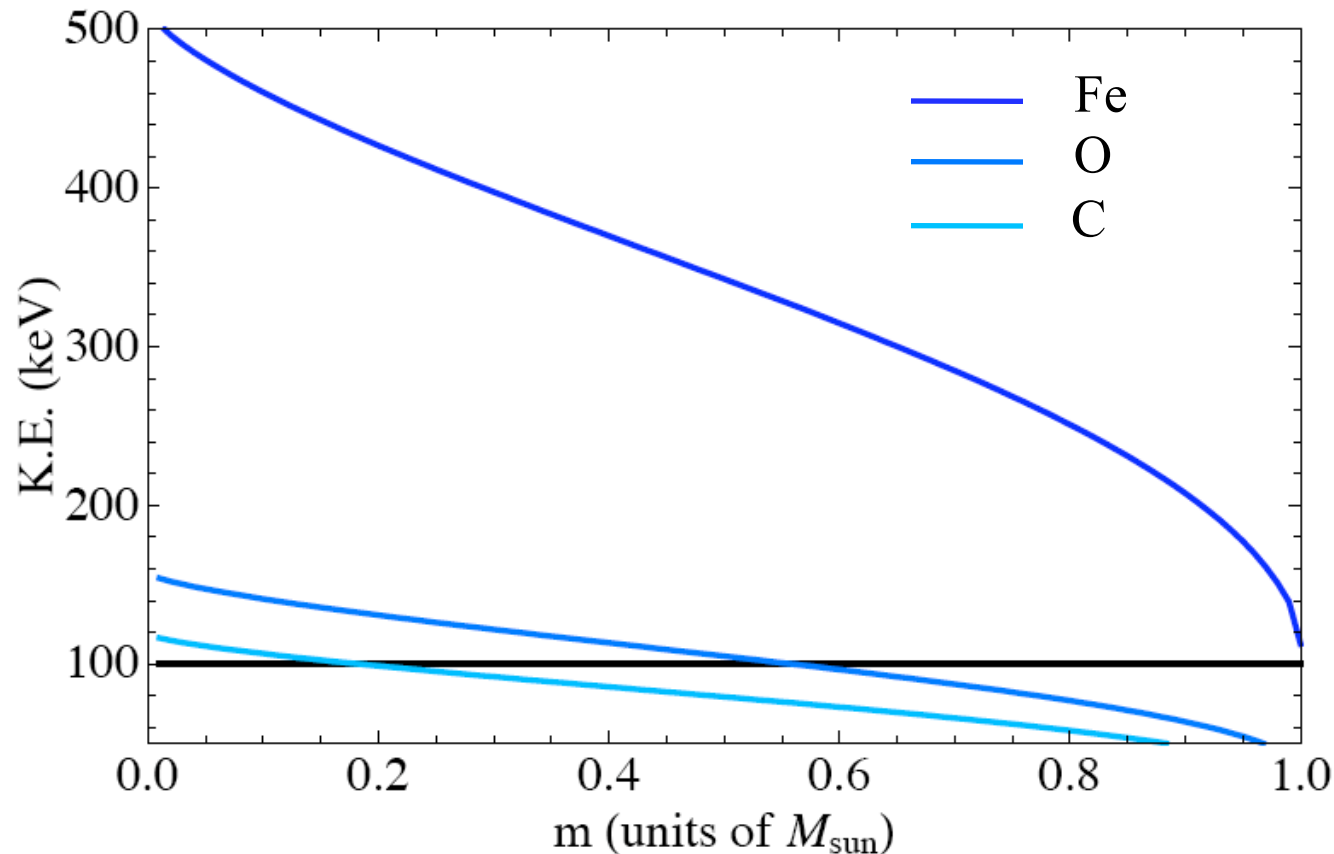
Nuclear Form Factors

For heavier elements, the WIMP no longer coherently scatters against the entire nucleus. This effect is captured by including a nuclear form factor,



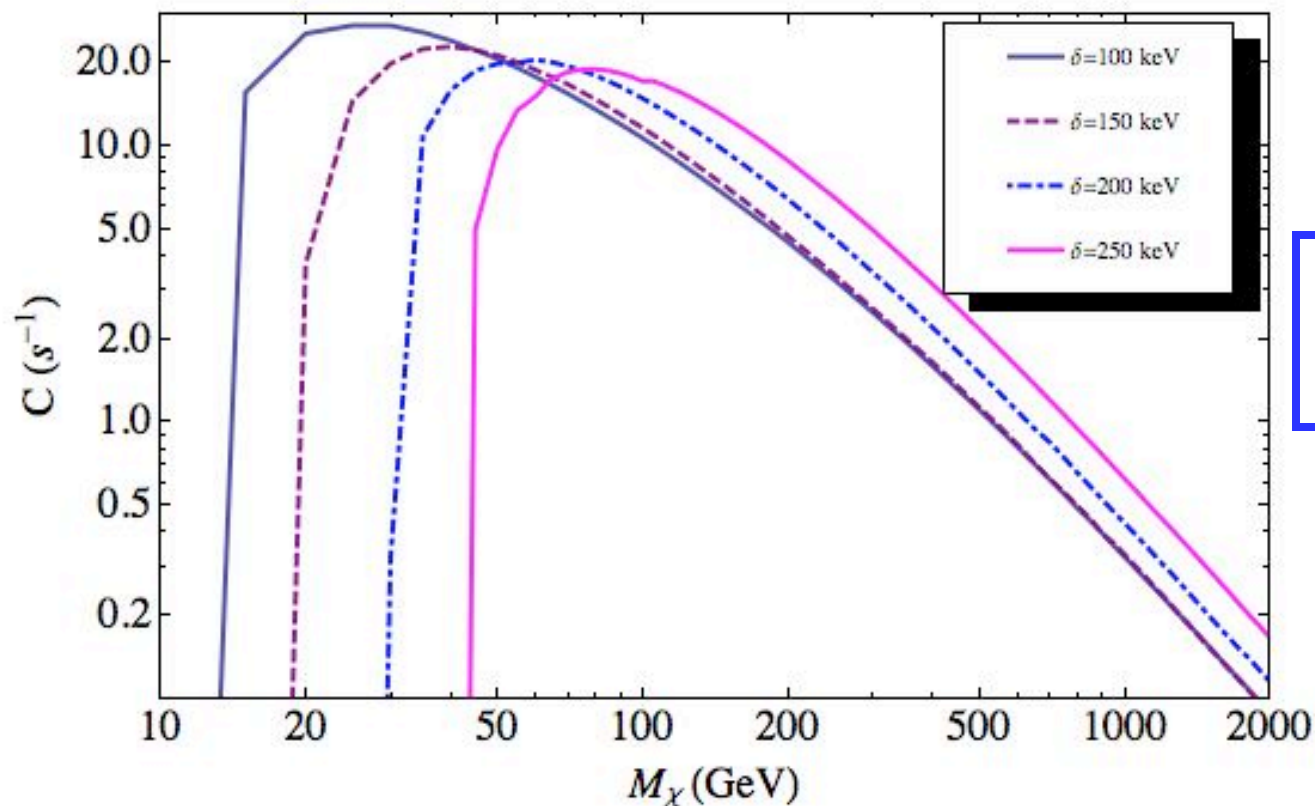
$$P_{cap} = \frac{1}{E_{max} - E_{min}} \int_{E_{cap}}^{E_{max}} e^{-E/E_0}$$

Which Elements Participate



$$M_{\chi} = 500 \text{ GeV} \quad u_{\infty} = 220 \text{ km/s}$$

Capture Rate



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It is easier to capture because some of the energy goes to excitation. Also, form-factor suppression is a little milder, especially for iron.

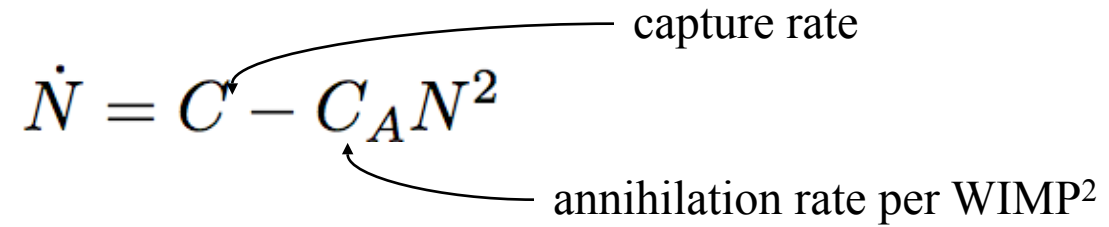
Annihilation Rate

The evolution of the WIMP population is governed by the equation,

$$\dot{N} = C - C_A N^2$$

capture rate

annihilation rate per WIMP²



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Is the solar lifetime long enough compared with the equilibrium time scale? **If not**, the signal is strongly reduced.

Equilibrium Time

$$C_A = \frac{\int d^3r \, n(r)^2 \, \langle \sigma_A v \rangle}{\left(\int d^3r \, n(r) \right)^2} \quad \text{And usually,} \quad n(r) = n_0 e^{-m_\chi \phi(r)/T}$$

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So, equilibrium has been reached long ago, and the signal is full strength.

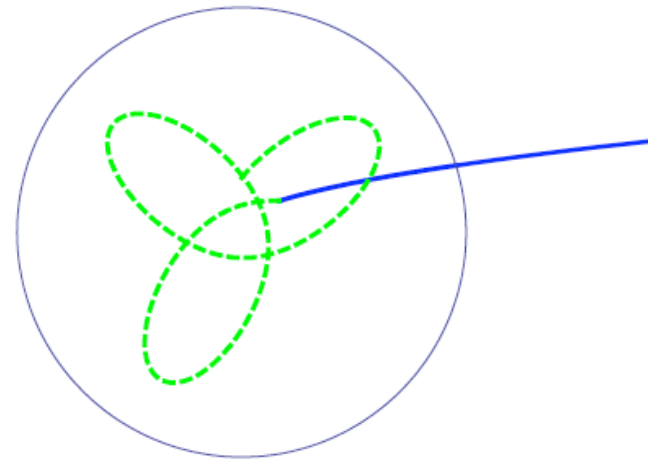
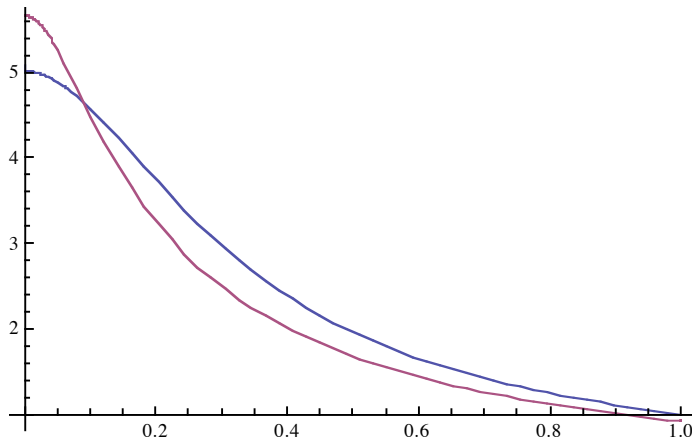
But, if the scattering is inelastic the WIMPs cannot thermalize!!! We need to compute the resulting density

Orbits

Henon (1959) found closed form solutions for the orbits of the following potential:

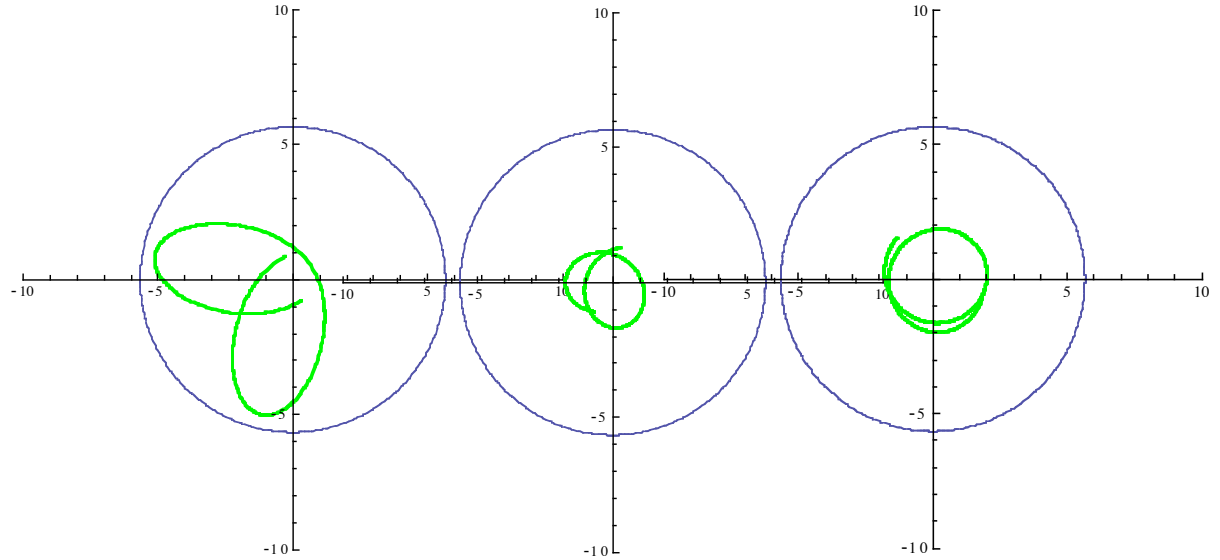
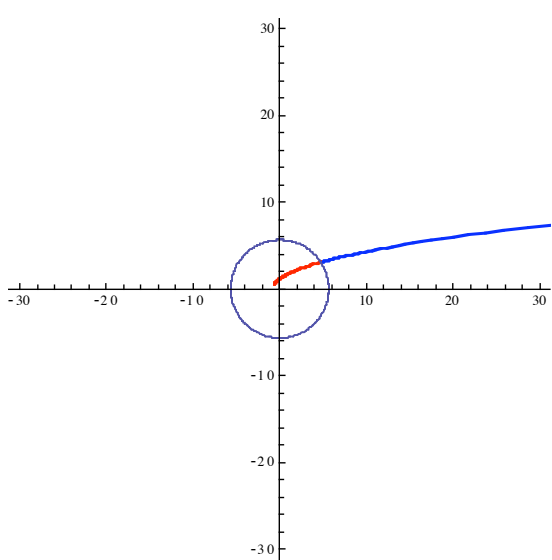
$$U(r) = \frac{GM_{\odot}m_{\chi}}{2bR_{\odot}} \left(1 - \frac{2b}{b + \sqrt{b^2 + r^2}} \right)$$

The potential in the sun can be fit fairly well to this potential,



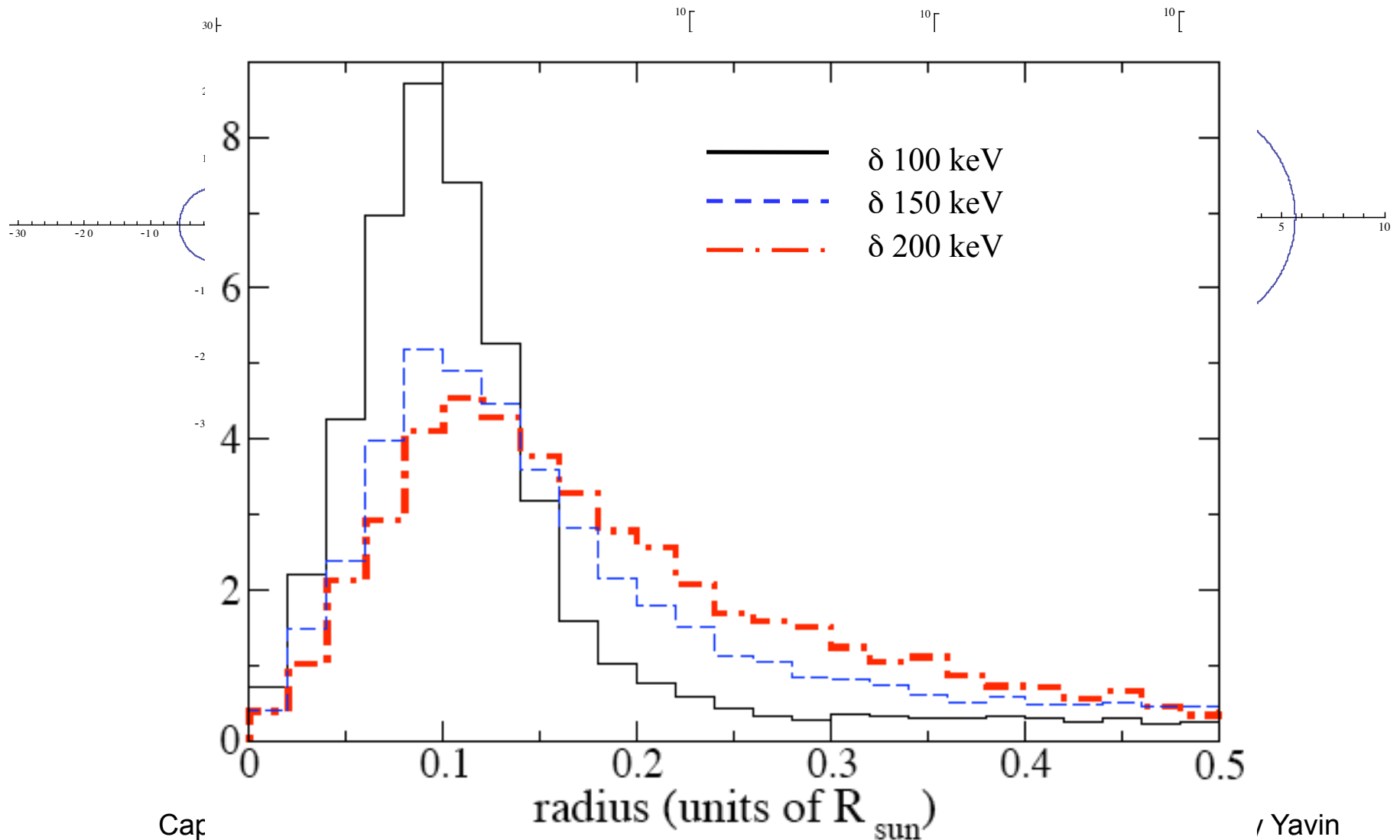
Density

The WIMP will keep on colliding until it lost enough energy so it no longer have enough energy to undergo an inelastic transition.



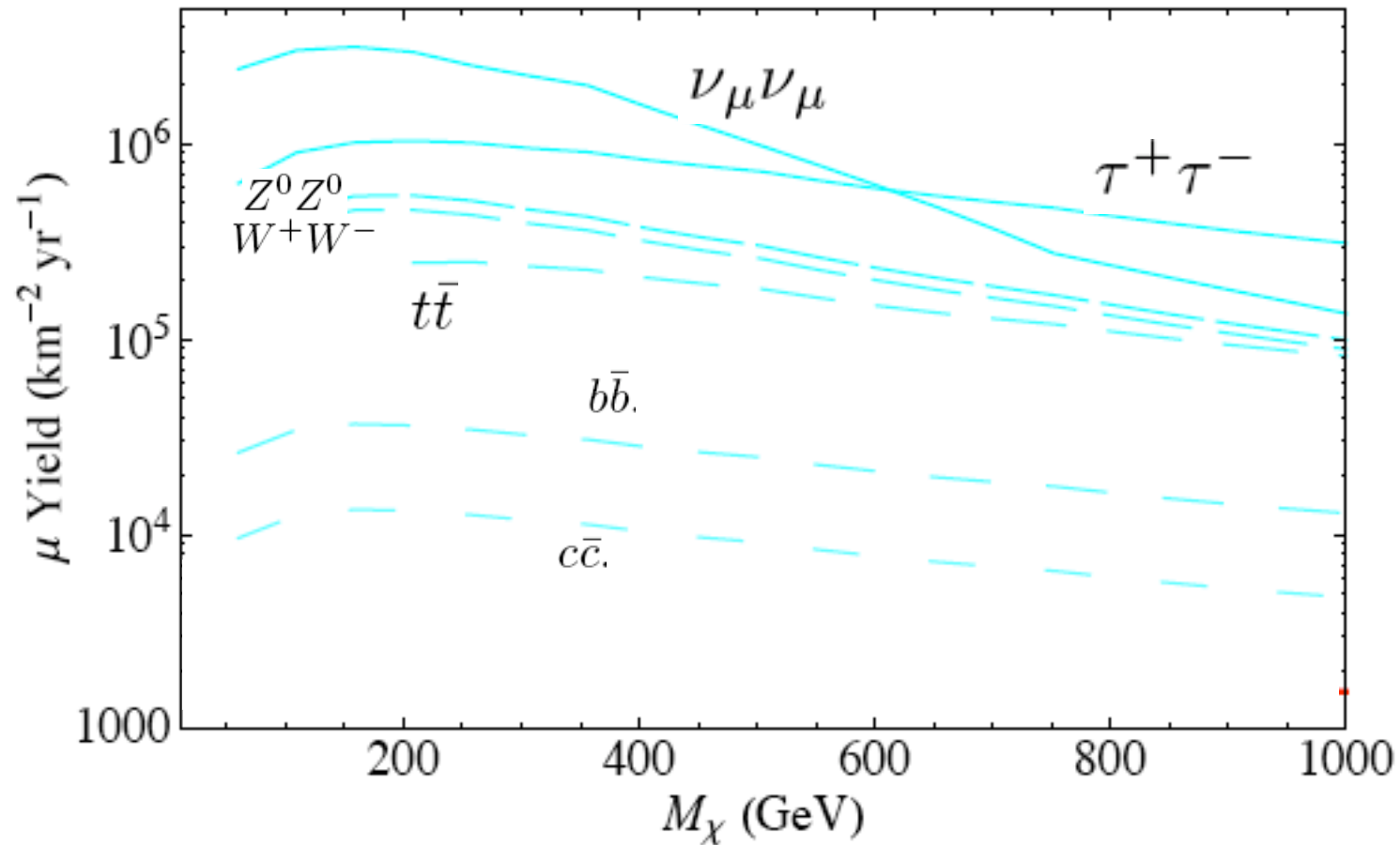
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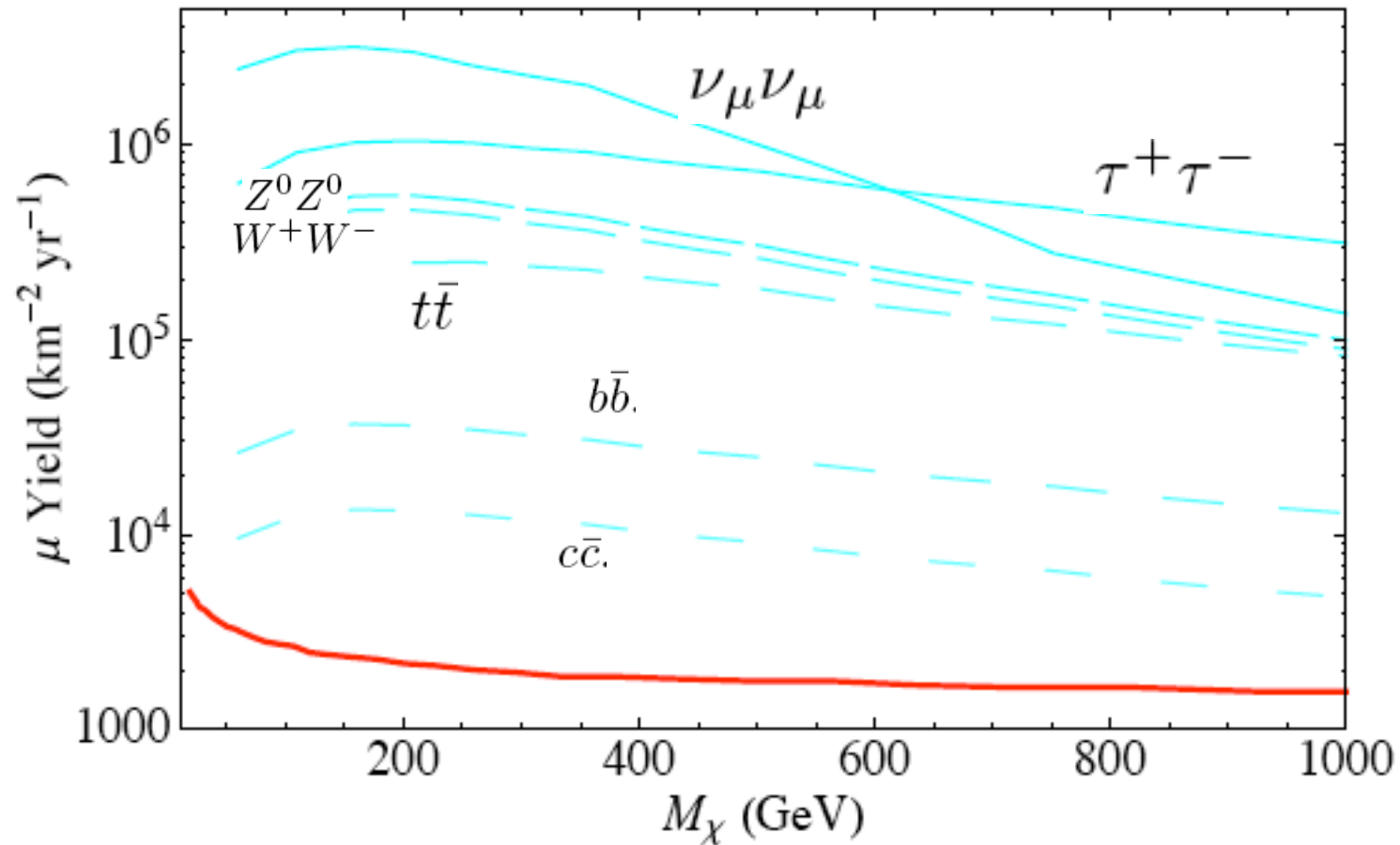
Muon Yield

To compute the resulting muon yield, we used DarkSUSY.
The inputs are: capture rate and annihilation channel.



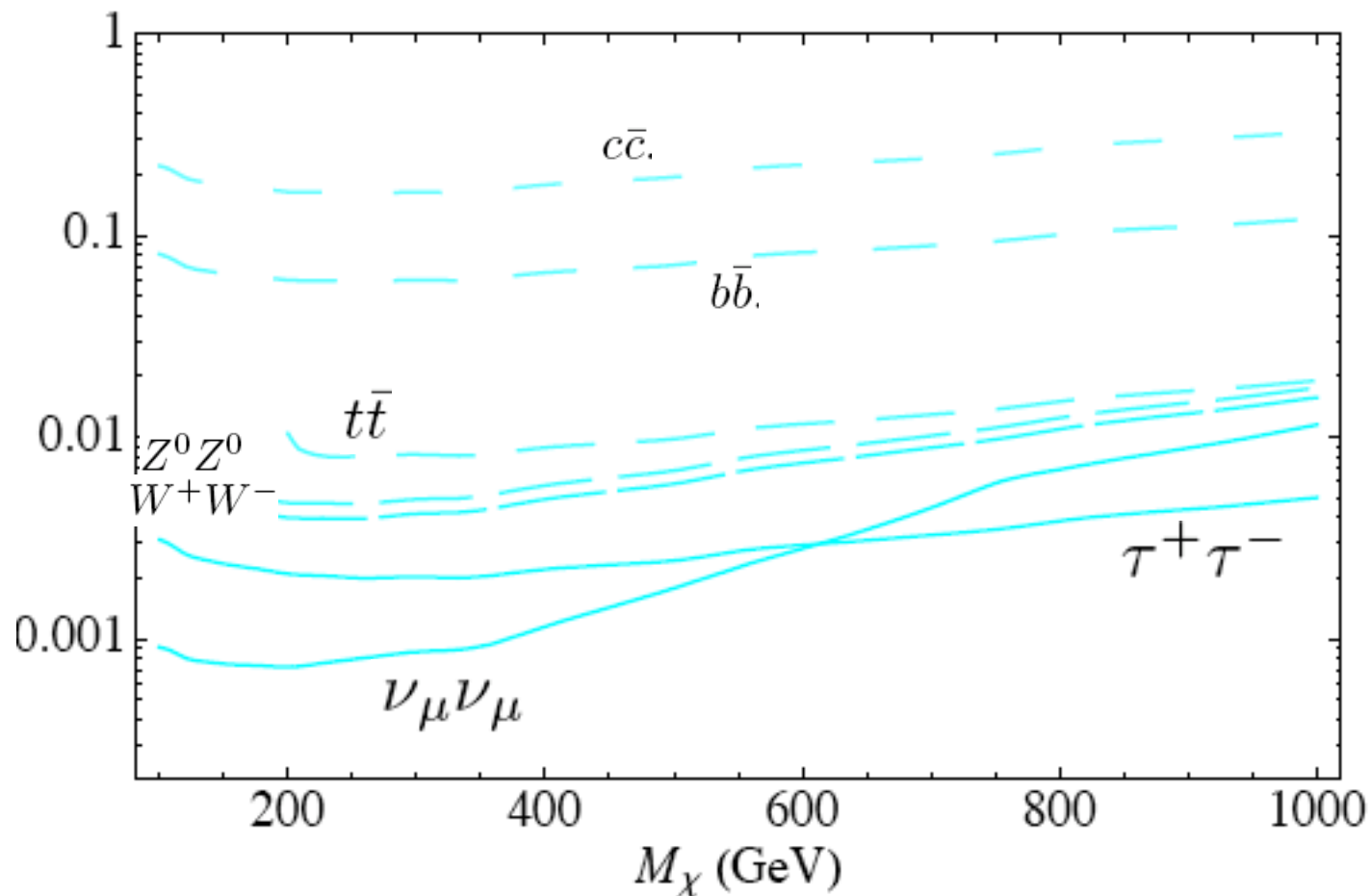
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Excluded Annihilation Channels

So, current bounds from Super-K, already allow us to place extremely stringent bounds on the annihilation channels of any such model.



Reaction 1

Well, I didn't believe DAMA's results to begin with so... pfff

Reaction 2

If you love the MSSM, then you would take it as a sign that iDM models are ruled out.

Reaction 3

Conservatively, we can say:
If iDM is ever verified, then we
know that DM annihilates in a very
peculiar way.

Dark Gauge Groups?

Suppose DM is charged under some new dark abelian group:

$$\mathcal{L} = \bar{\chi}\gamma^\mu D_\mu \chi + M\bar{\chi}\chi + \frac{1}{\Lambda}\chi h\chi h + \text{h.c.} \\ + |D_\mu h|^2 - V(h) - \frac{1}{4}f_{\mu\nu}f^{\mu\nu} \quad \langle h \rangle \approx \text{GeV}$$


$$\frac{\langle h \rangle^2}{\Lambda} \approx 100\text{keV}$$

Coupling to the SM can be achieved through kinetic mixing with hypercharge. Such a scenario will also yield the electron/positron excesses seen in PAMELA and possibly the CMB haze.

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- Inelastic DM models with generic couplings to the SM are excluded by neutrino telescopes.
- If DM is charged under some new abelian groups, PAMELA, ATIC and a few other observations can be accommodated. Inelastic scattering arises naturally and is NOT excluded by the present considerations.